

Verification of radical pair mechanism predictions for weak magnetic field effects on superoxide in planarians

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1 Abstract

2 Superoxide concentration and tissue regeneration in planarians exhibit a complex non-monotonic
3 dependence on the strength of an applied weak magnetic field. While this is difficult to un-
4 derstand based on classical physics, a recently proposed quantum model based on a flavin-
5 superoxide radical pair mechanism could replicate the previously observed superoxide concen-
6 trations. However, this model also predicts increased superoxide concentrations for both lower
7 and higher fields. This seemed to conflict with earlier experimental observations on blastema
8 sizes, which were correlated with superoxide in the previously observed regime but were known
9 not to follow the predicted trends for lower and higher fields. Motivated by this apparent
10 contradiction, we here directly experimentally tested the predictions of the quantum model
11 for superoxide for lower and higher fields. To our own surprise, our experiments confirmed
12 the predictions of the radical pair model for superoxide, and incorporating interactions with
13 multiple nuclei further improved the model's agreement with the experimental data. While
14 open questions remain regarding the exact relationship between blastema sizes and superoxide,
15 which is revealed to be more complex than previously observed, and the detailed properties of
16 the underlying radical pair, our results significantly support a quantum biological explanation
17 for the observed magnetic field effects.

18 1 Introduction

19 Hundreds of studies show that exposure to weak magnetic fields (WMFs), with a magnitude of
20 a few milliTesla (mT) or less, can influence many biological processes, even though the corre-
21 sponding magnetic energies are much weaker than the thermal energies at room temperature [1].
22 In particular, researchers have shown in multiple scenarios that the cellular production of reac-
23 tive oxygen species (ROS) is sensitive to WMFs [2–5]. In many other studies involving WMF
24 effects on higher-level processes, it has been shown that these effects are mediated by mod-
25 ulating ROS concentration [6–9]. ROS are biologically important derivatives of oxygen that
26 are vital for various cellular processes, including signaling [10] and include both free radicals
27 and non-radical species. Superoxide ($O_2^{\bullet-}$) and hydrogen peroxide (H_2O_2) are two of the most
28 important members of the ROS family.

29 Van Huizen et al. conducted a study involving planarian flatworms and found their regener-
30 ation to be sensitive to WMFs within the range of 0 – 600 μ T [11]. A subsequent study, Kinsey

31 et al., later extended this range to 900 μT [12]. Planarians have a large number of somatic
32 stem cells, which account for roughly a quarter of their total cell population [13]. Due to this
33 large adult stem cell population, they have an astonishing capability for regenerating all tissues,
34 including the central nervous system [14]. Van Huizen et al. observed that WMFs altered stem
35 cell proliferation and subsequent differentiation by changing ROS accumulation at the wound
36 site. Although these data established ROS-mediated WMF effects on planarian regeneration,
37 the specific ROS involved remained an open question. In a later study, $O_2^{\bullet-}$, but not H_2O_2 , was
38 identified as the specific ROS being modulated [12].

39 Given that, the corresponding energies for WMFs in this range are far smaller than thermal
40 energies at room temperature, no obvious classical explanation is available for these magnetic
41 field effects. However, the radical pair mechanism (RPM) [15, 16] is a potential quantum
42 mechanical explanation for such effects. The RPM involves the simultaneous creation of a
43 pair of radicals, for example, through the transfer of a single electron from one molecule to
44 another. A radical is a molecule that contains at least one unpaired electron. The spins of
45 the two unpaired electrons, one on each constituent molecule of the radical pair (RP), undergo
46 a transient coherent evolution. Depending upon the initial spin configuration of participating
47 molecules, RPs usually start in either singlet or triplet initial states. A system with a total
48 spin equal to 0 (1) has 1 (3) corresponding spin state(s) and is hence termed a singlet (triplet).
49 RPs interact with nearby nuclear spins through hyperfine (HF) interactions and with external
50 magnetic fields via the Zeeman interaction. As neither singlet nor triplet states are stationary
51 states of the spin Hamiltonian, these interactions cause singlet-triplet interconversion. Altering
52 the external magnetic field or substituting an isotope can modify this interconversion. A key
53 feature of the RPM is that the chemical products are spin-selective, with singlet and triplet
54 states leading to different outcomes. As a result, changes in the external magnetic field affect
55 the yields of products formed via the RPM.

56 In recent years, the RPM has been proposed as an explanation for several WMF effects in
57 biology [1, 17], including several experiments involving WMF effects on ROS production. Us-
58 selman et al. proposed a flavin and superoxide-based RPM to explain the effects of oscillating
59 magnetic fields at Zeeman resonance (1.4 MHz) on ROS production in human umbilical vein
60 endothelial cells [18]. A similar mechanism was used to explain the modulation of ROS produc-
61 tion in a hypomagnetic environment, which in turn affected neurogenesis in the hippocampal
62 region of mice [19].

63 In an earlier work, Rishabh et al. studied the possibility of an RPM-based mechanism to
64 explain the effects of WMFs on planarian regeneration [20]. In particular, they investigated the
65 viability of a flavin-superoxide-based radical pair mechanism to explain the observed modulation
66 of $O_2^{\bullet-}$ production by WMFs. They found that a triplet-born free radical pair can replicate the
67 previously observed magnetic field dependence for $O_2^{\bullet-}$. However, some of the predictions of
68 this model seemed to conflict with experimental observations on planarian new tissue growth
69 (blastema size) at hypomagnetic and higher field values (500 – 900 μT). The blastema is
70 a collection of undifferentiated adult stem cell progeny that arises in response to injury and
71 serves as the basis for new tissues during regenerative growth.

72 Here, we set out to test these predictions of the RPM in planarians for WMF effects on
73 $O_2^{\bullet-}$ levels. Since data on $O_2^{\bullet-}$ levels were not available for these field strengths, we performed
74 new measurements to test the radical pair model's predictions for $O_2^{\bullet-}$ under these conditions.
75 Our experiments confirmed the theoretical predictions for $O_2^{\bullet-}$ behavior. These results also imply
76 that the interrelationship between $O_2^{\bullet-}$ levels and blastema size is nonlinear and more complex
77 than previously thought. Going beyond previous modeling work, we found that incorporating
78 HFIs with multiple nuclei improved the agreement between the theoretical predictions and the
79 experimental observations. Although there remain some open questions regarding an RPM-
80 based modulation of $O_2^{\bullet-}$ during planarian regeneration, this study significantly supports the
81 possibility of such an underlying mechanism.

82 2 Relevant prior results

83 2.1 Prior Experimental data (Ref. [11, 12])

84 Van Huizen et al. [11] reported that WMFs alter stem cell proliferation and differentiation,
85 hence regulating blastema formation following amputation in planarians. These effects were
86 dependent on field strength across a wide range, with maximum effects seen at 200 and 500 μT .
87 Significant reductions in blastema size were observed for 200 μT , while a substantial increase
88 was seen at 500 μT .

89 The observations of Van Huizen et al. [11] also highlighted the importance of ROS, which
90 peak at the wound site 1 hour post injury. They found that pharmacological inhibition with
91 the general ROS inhibitor diphenyleneiodonium resulted in a considerable decrease in blastema
92 size. Moreover, they found that by inhibiting superoxide dismutase (SOD), an enzyme that
93 catalyzes $\text{O}_2^{\bullet-}$ removal, they were able to rescue blastema growth in 200 μT fields. They also
94 found that SOD inhibition significantly increases blastema size in planarians exposed to control
95 geomagnetic conditions. Based on this evidence, they hypothesized that WMF effects were
96 mediated by changing ROS concentrations. To confirm this hypothesis, they measured the ROS
97 levels using a general oxidative stress indicator dye at 1 hour after injury for worms exposed to
98 200 and 500 μT fields. As expected, measurements at 200 μT revealed a significant decrease in
99 ROS levels, whereas at 500 μT , they saw significantly increased ROS concentrations.

100 To gain a better understanding of the specific targets of WMFs, Kinsey et al. [12] studied the
101 effects of WMF exposure on $\text{O}_2^{\bullet-}$ and H_2O_2 levels during planarian regeneration. They exposed
102 amputated planarians to 200 and 500 μT and then measured $\text{O}_2^{\bullet-}$ levels using a superoxide-
103 specific indicator dye at 1 and 2 hours after injury. $\text{O}_2^{\bullet-}$ concentrations were found to be
104 sensitive to WMFs in a fashion similar to WMF effects on ROS-mediated stem cell activity.
105 They reported that $\text{O}_2^{\bullet-}$ concentration decreased for worms exposed to 200 μT at both 1 and 2
106 hours post amputation. In contrast, while no significant change was observed for 500 μT fields
107 after 1 hour, a substantial increase was recorded at 2 hours post-amputation. The WMF effects
108 on $\text{O}_2^{\bullet-}$ levels for both these field values were significantly greater 2 hours after amputation than
109 1 hour after. Their $\text{O}_2^{\bullet-}$ measurements at 2 hours are reproduced in Fig. 2a. It should also be
110 noted that they did not observe any significant changes in H_2O_2 concentration as compared to
111 geomagnetic control. Based on these findings, Kinsey et al. concluded that WMF effects on
112 planarian regeneration are mediated at least in part via $\text{O}_2^{\bullet-}$.

113 2.2 Theoretical modeling of prior experimental data (Ref. [20])

114 Can an RPM-based $\text{O}_2^{\bullet-}$ production scheme explain the above observations? As the sign in-
115 version in the product yields at low fields is expected for the RPM, it is not unreasonable to
116 contemplate the existence of such a mechanism [16, 21–23]. To answer the above question,
117 Rishabh et al. [20] compared the predictions of a potential RPM model for $\text{O}_2^{\bullet-}$ yield with the
118 effects observed by Kinsey et al. for 200 and 500 μT exposures. A detailed summary of the
119 main findings is provided below. Before we proceed, it should be noted that the observational
120 techniques available for superoxide measurement in live planarians provide relative concentra-
121 tions rather than precise values. Therefore, we will restrict our comparison to the shape of the
122 magnetic field profile rather than the exact values of these effects.

123 The two primary cellular sources of $\text{O}_2^{\bullet-}$ are the mitochondrial electron transport chain
124 and a membrane enzyme family called NADPH oxidase (Nox) [24–27]. In mitochondria, most
125 $\text{O}_2^{\bullet-}$ is produced at two sites in complex I and one in complex III. Of the two chemical processes
126 responsible for $\text{O}_2^{\bullet-}$ production in mitochondrial complex I, one involves an electron transfer from
127 the reduced form of flavin mononucleotide (FMNH^-) to molecular oxygen (O_2) forming $\text{O}_2^{\bullet-}$ and
128 FMNH^\bullet [28]. Nox are flavohemoproteins and electron transporters, and Nox1-3 and Nox5 are
129 known to produce $\text{O}_2^{\bullet-}$. This involves an electron transfer from FADH^- to O_2 , occupying a

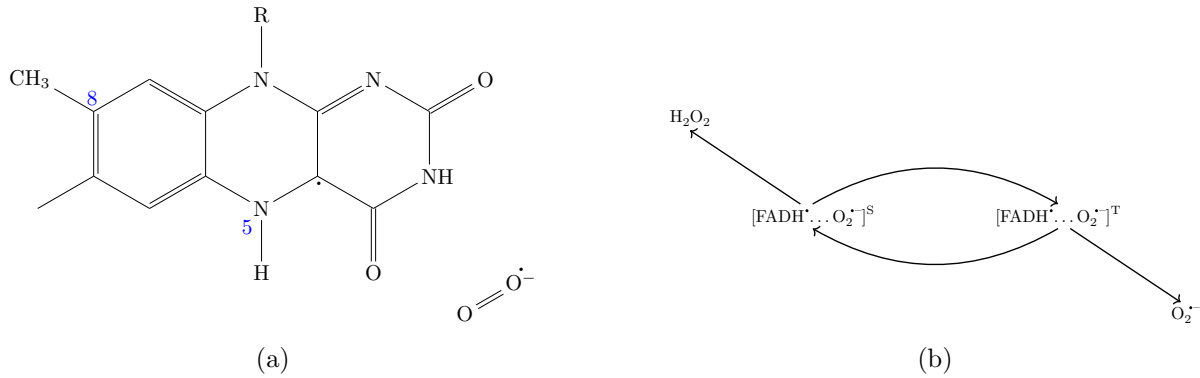


Figure 1: **Radical pair model:** (a) Flavin-superoxide radical pair. (b) Radical pair reaction scheme. Triplet and singlet products are $\text{O}_2^{\bullet-}$ and H_2O_2 , respectively. In this study we consider the following five isotropic HF couplings for FH^\bullet : H5 ($-802.9 \mu\text{T}$), N5 ($431.3 \mu\text{T}$), three H8 ($255.4 \mu\text{T}$) [30].

130 binding site near the heme groups [29]. The electron transfers from fully reduced flavin to
 131 O_2 during the production of $\text{O}_2^{\bullet-}$ in both mitochondria and Nox, as well as the magnetic field
 132 dependence of $\text{O}_2^{\bullet-}$ production, suggest the involvement of a flavin-superoxide RP ($[\text{FH}^\bullet \cdots$
 133 $\text{O}_2^{\bullet-}]$). This FH^\bullet and $\text{O}_2^{\bullet-}$ based RPM can serve as the basis for explaining various WMF effects
 134 observed in the context of $\text{O}_2^{\bullet-}$ production [6, 12].

135 Following Usselman et. al.[18], a triplet-born RP system of FH^\bullet and $\text{O}_2^{\bullet-}$ (See Fig. 1a) was
 136 proposed with triplet and singlet products being $\text{O}_2^{\bullet-}$ and H_2O_2 , respectively (See Fig. 1b). The
 137 singlet and triplet reaction rates are denoted by k_S and k_T , respectively. The spin relaxation
 138 rates of radicals A and B are denoted by r_A and r_B , respectively.

139 To study the RP dynamics, a simplified spin Hamiltonian including only the Zeeman and
 140 largest isotropic HF coupling for FH^\bullet was considered:

$$\hat{H} = \omega \hat{S}_{A_z} + \omega \hat{S}_{B_z} + a_1 \hat{\mathbf{S}}_A \cdot \hat{\mathbf{I}}_1, \quad (1)$$

141 where \hat{S}_{A_z} and \hat{S}_{B_z} are the spin-z operators of radical electron A (FH^\bullet) and B ($\text{O}_2^{\bullet-}$), respectively,
 142 ω is the Larmor precession frequency of the electrons due to the Zeeman effect, $\hat{\mathbf{S}}_A$ is the spin
 143 vector operator of radical electron A, $\hat{\mathbf{I}}_1$ is the nuclear spin vector operator of the H5 of FH^\bullet ,
 144 and a_1 is the isotropic HF coupling constant (HFCC) between the H5 of FH^\bullet and the radical
 145 electron A ($a_1 = -802.9 \mu\text{T}$) [30]. H5 has by far the largest isotropic HFCC among all the
 146 nuclei in FH^\bullet [30].

147 The fractional triplet ($\text{O}_2^{\bullet-}$) yield generated by the RPM can be determined by monitoring
 148 the dynamics of RP spin states. For details of the calculations, see the Methods section.
 149 The ultimate fractional triplet yield ($\Phi_T^{(T)}$) for an RP that originates in a triplet state, when
 150 considering time intervals significantly longer than the RP's lifetime, is as follows:

$$\Phi_T^{(T)} = k_T \text{Tr} \left[\hat{P}^T \hat{L}^{-1} \left[\frac{1}{3M} \hat{P}^T \right] \right], \quad (2)$$

151 where \hat{L} is the Liouvillian superoperator, \hat{P}^T is the triplet projection operator, M is the total
 152 number of nuclear spin configurations, and k_T is the triplet reaction rate.

153 There are four free parameters in this model, namely, k_S , k_T , r_A , and r_B . The question was
 154 whether there are regions in parameter space where the simulated behavior corresponds to the
 155 experimental observation (i.e., a positive change in $\Phi_T^{(T)}$ at $500 \mu\text{T}$ and a negative change at
 156 $200 \mu\text{T}$ with respect to geomagnetic control). For this purpose, Rishabh et al. investigated the
 157 signs of triplet yield changes with respect to control at $200 \mu\text{T}$ and $500 \mu\text{T}$ over a wide range
 158 of chemical reaction rates ($k_S \in \{10^4 \text{ s}^{-1}, 10^7 \text{ s}^{-1}\}$ and $k_T \in \{10^4 \text{ s}^{-1}, 10^7 \text{ s}^{-1}\}$) for various

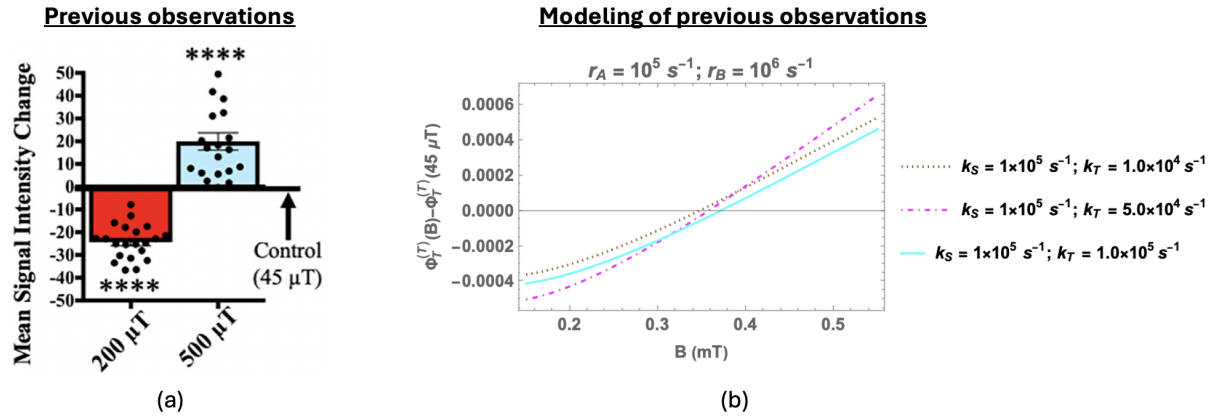


Figure 2: **Summary of relevant prior results:** (a) Superoxide ($O_2^{\bullet-}$) measurements at the wound site 2 hours after amputation (reproduced from [12]). 200 (red) and 500 (blue) μT exposures each relative to 45 μT geomagnetic controls. Significance: Student’s t-test. **** $p < 0.0001$. (b) Change in the fractional triplet yield for triplet-born flavin-superoxide RP with respect to the geomagnetic control (45 μT) as a function of the magnetic field (150 – 550 μT) [20]. Here, only the largest isotropic HF coupling (H5) is taken into account (HFCC value is $-802.9 \mu\text{T}$). $r_A = 10^5 \text{ s}^{-1}$ and $r_B = 10^6 \text{ s}^{-1}$. k_S and k_T are singlet and triplet reaction rates, respectively. r_A and r_B are the spin relaxation rates of radicals A and B, respectively.

159 pairs of spin relaxation rates r_A and r_B . They observed that such a region in k_S - k_T plane can
 160 be found provided $r_A \leq 10^5 \text{ s}^{-1}$ and $r_B \leq 10^6 \text{ s}^{-1}$.

161 Fig. 2b shows the change in $\Phi_T^{(T)}$ with respect to the geomagnetic control as a function of
 162 the magnetic field for various values of k_S and k_T when r_A is fixed at $1 \times 10^5 \text{ s}^{-1}$ and r_B is
 163 fixed to $1 \times 10^6 \text{ s}^{-1}$. It is clear that for appropriate rate values, Rishabh et al.’s RP model
 164 can replicate the previously observed magnetic field dependence, including the sign change.
 165 However, it should be noted that the magnitude of the observed effects is much larger than
 166 what could be achieved by any RP model. This highlights the necessity of an amplification
 167 mechanism, as discussed by Rishabh et al. We will revisit this issue in the discussion section.

168 2.3 Predictions of the radical pair model

169 Beyond 500 μT

170 As shown in Fig. 3 (yellow shaded region), the RPM predicts that as we increase the magnetic
 171 field strength beyond 500 μT , we should observe a corresponding rise in $O_2^{\bullet-}$ levels. Note that,
 172 the exact amount of this rise will depend on the specific parameters of the model.

173 Hypomagnetic effects

174 In an RPM, the fractional triplet yield can also be altered by shielding the geomagnetic field [31].
 175 The effect on the fractional triplet yield of the RPM of shielding geomagnetic field for a triplet-
 176 born RP is shown in Fig. 3 (green shaded region). These simulations suggest a positive change
 177 in a hypomagnetic environment. The exact size of the effect will again depend on the specific
 178 parameters of the model [19, 31].

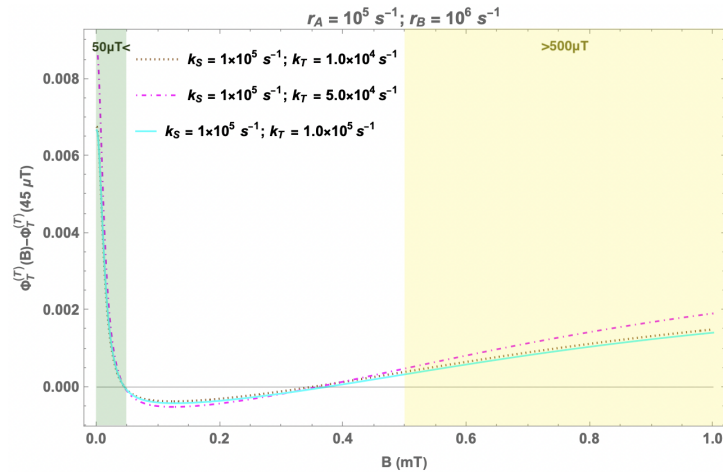


Figure 3: **Predictions of the RPM model:** Change in the fractional triplet yield for triplet-born flavin-superoxide RP with respect to the geomagnetic control ($45 \mu\text{T}$) as a function of the magnetic field ($0 - 1 \text{ mT}$). $r_A = 10^5 \text{ s}^{-1}$ and $r_B = 10^6 \text{ s}^{-1}$. k_S and k_T are singlet and triplet reaction rates, respectively. r_A and r_B are the spin relaxation rates of radicals A and B, respectively. Again, only the largest isotropic HF coupling (H5) is taken into account (HFCC value is $-802.9 \mu\text{T}$). The region with sub-geomagnetic fields is shaded in green, and the region with fields greater than $500 \mu\text{T}$ is shaded in yellow.

179 3 Results

180 3.1 Measurement of magnetic field effects on superoxide

181 Despite the fact that the predictions of the flavin-superoxide RP model can align with the
 182 observed behavior of $\text{O}_2^{\bullet-}$ at 200 and $500 \mu\text{T}$, its predictions at the hypomagnetic and higher
 183 fields might raise serious doubts about the viability of the model. Kinsey et al. measured the
 184 effects of hypomagnetic and higher fields ($600\text{-}900 \mu\text{T}$) on blastema size and general ROS, but
 185 not specifically on $\text{O}_2^{\bullet-}$. Their observations showed no significant effects (except at $900 \mu\text{T}$)
 186 for these fields. If similar patterns are reflected in $\text{O}_2^{\bullet-}$ levels, it would challenge the current
 187 model unless some deamplification mechanism is activated (or the amplification mechanism is
 188 deactivated) when $\text{O}_2^{\bullet-}$ levels become too high. According to the existing hypothesis regarding
 189 $\text{O}_2^{\bullet-}$ mediation of WMF effects on planarian regeneration, it is expected that $\text{O}_2^{\bullet-}$ levels should
 190 follow a behavior similar to that of blastema size. Therefore, to settle the question of the
 191 involvement of the RPM, we conducted measurements of $\text{O}_2^{\bullet-}$ levels at 700 and $900 \mu\text{T}$, as well
 192 as at hypomagnetic field values. To our surprise, the experiments confirmed the theoretical
 193 predictions of the RP model concerning the behavior of superoxide at hypomagnetic and larger
 194 fields, contrary to expectations based on earlier experimental observations on blastema sizes.

195 Fig. 4 shows the results of these experiments. Adult *Schmidtea mediterranea* planarians
 196 were amputated above the pharynx (feeding tube) to produce fragments that undergo head
 197 regeneration as illustrated in Fig. 4a. Regenerates were exposed to static WMFs at $0, 200, 500,$
 198 700 and $900 \mu\text{T}$ for the first 2 hours post amputation. The superoxide-specific live reporter dye,
 199 orange 1, was used to visualize $\text{O}_2^{\bullet-}$ concentrations at the wound site at 2 hours post injury (the
 200 peak of superoxide accumulation) as in Fig. 4b. Quantification of these data is shown in Fig.
 201 4c, demonstrating that similar to previous findings [12], $200 \mu\text{T}$ significantly inhibited while 500
 202 μT significantly increased superoxide levels as compared to geomagnetic controls. However, in
 203 contrast to those investigations of general ROS and blastema size, examination revealed that
 204 $\text{O}_2^{\bullet-}$ concentrations are also significantly increased at $0, 700,$ and $900 \mu\text{T}$. Furthermore, the
 205 peak average increase in $\text{O}_2^{\bullet-}$ occurred with $0 \mu\text{T}$ exposure, as predicted by the RP model.
 206 Together, these experimental results demonstrate that WMFs alter superoxide concentration at

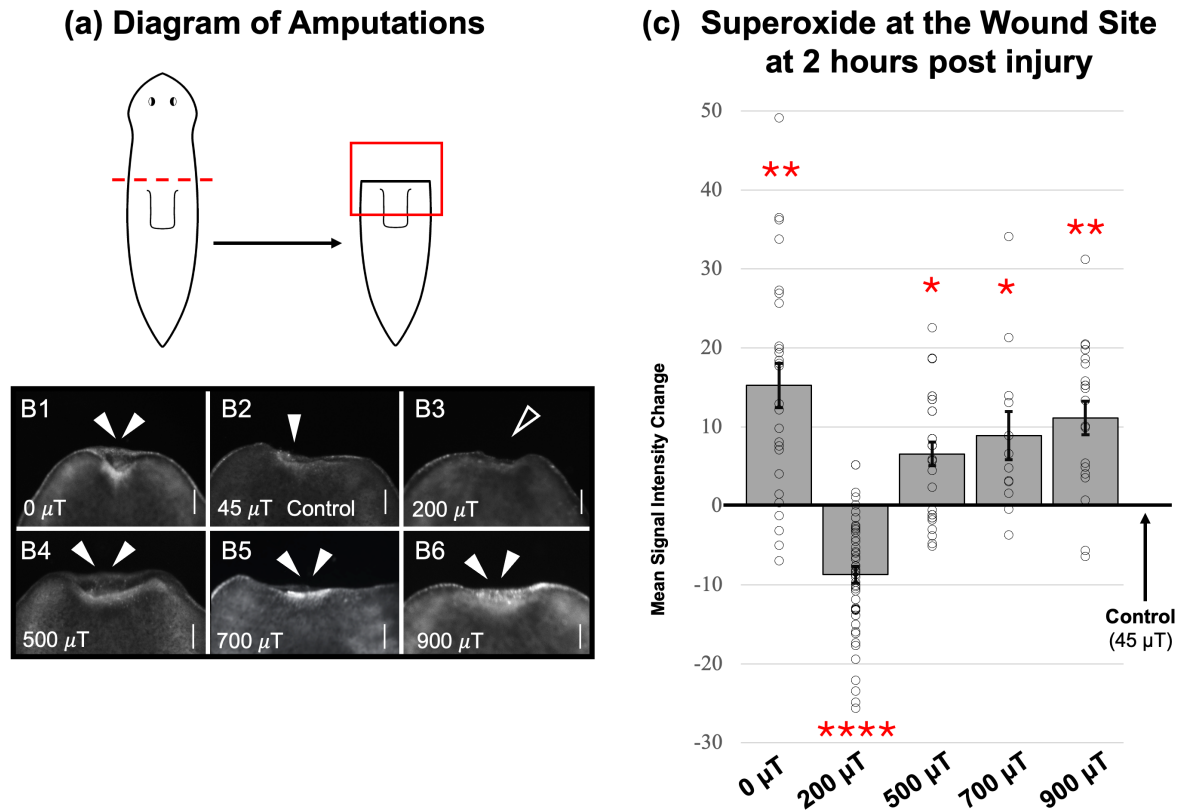


Figure 4: **Validation of RPM predictions:** Regenerating *S. mediterranea* planarians 2 hours after injury, exposed to a range of static WMFs. (a) Diagram of amputation (dotted red line). Red box represents region as shown in b which corresponds to the anterior wound site. (b) $O_2^{\cdot-}$ accumulation visualized by orange 1 live reporter dye. Control = 45 μT (B2, geomagnetic average). Solid arrow = normal $O_2^{\cdot-}$ levels. Double arrows = increased and open arrow = inhibited $O_2^{\cdot-}$ levels (as compared to control). Scale bars = 100 μm . Anterior is up. (c) Quantification of b, with changes in signal intensity relative to 45 μT controls. $n \geq 12$ for all. Significance: Student's t-test. * $p < 0.02$, ** $p < 0.005$, **** $p < 0.0001$.

207 the wound site in a field strength dependent manner consistent with the RP model.

208 3.2 Multiple hyperfine interactions

209 Although Rishabh et al.'s model correctly predicted the sign of WMF effects, it significantly
 210 overestimates the impact of hypomagnetic fields compared to higher field values. We found that
 211 this is, in part, an artifact of the simplifying assumption of including only one HFI. Bringing
 212 the RP model closer to reality by taking into account isotropic HFIs with multiple nuclei (not
 213 just the largest one as in the previous work by Rishabh et al.) leads to a much-improved
 214 correspondence between the predictions of the theoretical model and the observations from the
 215 experiments. Fig. 5 shows the theoretical predictions of our model with five HFIs. We have
 216 taken into account the five nuclei with the largest isotropic HFCCs, namely: H5 ($-802.9 \mu T$),
 217 N5 ($431.3 \mu T$), three H8 ($255.4 \mu T$) [30]. Note that introducing a second HFI had significant
 218 effects, but adding additional HFIs beyond that had little impact. This is shown in Fig. 6 in the
 219 supporting information. At this point, let us also note that, despite the introduction of multiple
 220 HFIs, the agreement between theory and experiment—though significantly improved—is still
 221 not perfect. While it is difficult to pinpoint the exact cause of this mismatch, it may stem from
 222 the amplification chemistry or the observational techniques used for measuring superoxide.

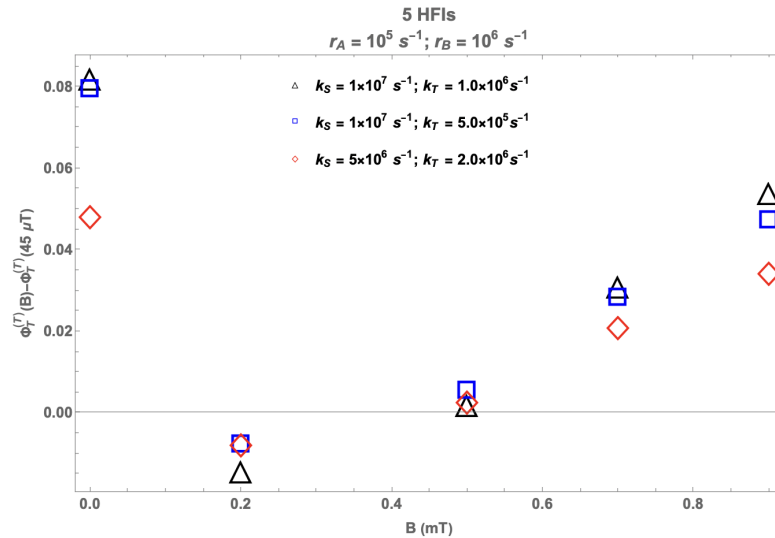


Figure 5: **Multiple HFIs:** Change in the fractional triplet yield for triplet-born RP with respect to the geomagnetic control (45 μT) as a function of the magnetic field. $r_A = 10^5 \text{ s}^{-1}$ and $r_B = 10^6 \text{ s}^{-1}$. k_S and k_T are singlet and triplet reaction rates, respectively. r_A and r_B are the spin relaxation rates of radicals A and B, respectively. 5 HFIs: H5 ($-802.9 \mu\text{T}$), N5 ($431.3 \mu\text{T}$), three H8 ($255.4 \mu\text{T}$) [30].

223 4 Discussion

224 In this work, we set out to test the predictions of a $[\text{FH}^{\bullet} \cdots \text{O}_2^{\bullet-}]$ RP-based model for WMF
 225 effects on $\text{O}_2^{\bullet-}$ levels during planarian regeneration. It was known that a triplet-born free
 226 radical pair can replicate the previously observed magnetic field dependence, including the sign
 227 change [20]. However, the model's predictions at hypomagnetic and higher fields did not align
 228 with the expected behavior of $\text{O}_2^{\bullet-}$ based on prior observations of blastema size. Surprisingly,
 229 our experiments confirmed the predictions of the radical pair model concerning the behavior
 230 of superoxide at hypomagnetic and larger fields. Moreover, extending previous models, we
 231 found that taking into account isotropic HFIs with multiple nuclei leads to a much-improved
 232 correspondence between the RP model's predictions and the experimental data. These results
 233 strongly suggest the possibility of an underlying RPM.

234 These results also highlight the complex interrelation between $\text{O}_2^{\bullet-}$ and tissue regeneration
 235 in planarians. As mentioned above, the blastema size, measured by Kinsey et al. [12], does not
 236 emulate the behavior of superoxide concentration at the wound site, in particular for 0 and 700
 237 μT . This non-linear relationship between new tissue growth and superoxide levels after injury
 238 may be related to the fact that superoxide accumulation occurs in the first hours after injury,
 239 while blastema growth occurs between 24-72 hours [32]. Teasing apart the exact relationship
 240 between early ROS and tissue regrowth should be a focus of studies going forward.

241 It should be noted that despite the successful predictions of this RP model regarding the
 242 superoxide levels, some open questions remain. We highlight some of the main issues in this and
 243 the following paragraphs. The usual singlet product of the $[\text{FH}^{\bullet} \cdots \text{O}_2^{\bullet-}]$ RP is H_2O_2 [18, 19].
 244 However, Kinsey et al. [12] did not observe any significant effect of WMF on H_2O_2 concentration.
 245 This suggests that either H_2O_2 is not the main singlet product in the present case, or more
 246 probably, it indicates the absence of an amplification process for H_2O_2 .

247 It has been suggested in the past that due to fast molecular rotation, free $\text{O}_2^{\bullet-}$ should have
 248 a spin relaxation lifetime on the orders of 1 ns and hence a fast spin relaxation rate r_B [33,
 249 34]. The relaxation rate requirement calculated by our model for r_B is significantly lower than
 250 this expected value. However, this fast spin relaxation of free superoxide can be lowered if

251 the molecular symmetry is reduced and the angular momentum is quenched by the biological
252 environment [33, 34]. Although, it should be noted that for this to happen $O_2^{\bullet-}$ must be tightly
253 bound [34]. Such a possibility may arise in the case of the Nox enzyme because of the pres-
254 ence of O_2 binding pockets near the heme proteins. However, it should be noted that tightly
255 bound flavin molecules, which require consideration of anisotropic rather than isotropic hyper-
256 fine coupling, cannot explain experimental observations [20]. This strongly suggests that the
257 $O_2^{\bullet-}$ involved is not produced via Nox, or the flavin bound to Nox is unexpectedly still relatively
258 free to rotate. It has also been indicated that O_2 would need to bind in the mitochondrial
259 electron transfer flavoprotein for superoxide production [35]. Direct evidence of such inhibition
260 of spin relaxation (for example, an electron paramagnetic resonance spectrum of $O_2^{\bullet-}$) has yet
261 to be found.

262 Despite predicting the correct behavior of magnetic field effects, the RPM model alone can
263 not predict the right size of these effects and does not account for the temporal aspect of Kinsey
264 et al.'s [12] observation. This illustrates the need for an amplification process for $O_2^{\bullet-}$ [20]. The
265 existence of Ca^{2+} - $O_2^{\bullet-}$ self-amplifying loop [36] and JNK- $O_2^{\bullet-}$ amplification pathway [37], and the
266 fact that such a pathway is activated precisely during regeneration [38] adds to the plausibility
267 of such an amplification process.

268 It should also be pointed out that we have ignored inter-radical interactions in our modeling.
269 The effects of including exchange interaction have been studied in Ref. [20] and do not change
270 our main conclusions.

271 In this study, we have only considered triplet-born free RPs. However, other related possi-
272 bilities, such as F-pairs and radical triads, cannot be ruled out [20]. Moreover, the possibility
273 that these WMF effects may be due to some other RP, such as flavin-tryptophan, can not be
274 completely excluded. The production of $O_2^{\bullet-}$, in that case, might happen downstream of the
275 RP spin dynamics [39]. However, it should be noted that there is no strong biological reason
276 to believe the involvement of such RPs in $O_2^{\bullet-}$ production during planarian regeneration. For
277 example, it remains unclear whether CRY, a natural host of flavin-tryptophan RP, plays any
278 role in planarians. It is also possible that mechanisms other than the RPM could also explain
279 the WMF effects on planarians.

280 In summary, although further investigation is needed to conclusively prove the involvement
281 of a radical pair in planarian regeneration or to determine the exact nature of such a pair,
282 the experimental verification of RPM's predictions regarding superoxide levels in this study
283 provides significant support to the possibility of such an underlying quantum mechanism.

284 5 Methods

285 5.1 Radical pair mechanism calculations

286 The state of the RP is described using the spin density operator. The coherent spin dynamics,
287 chemical reactivity, and spin relaxation all together determine the time evolution of the spin
288 density matrix of the RP system.

289 Since the ground state of the oxygen molecule is a triplet, we will consider the initial state
290 of the RP to be a triplet:

$$\frac{1}{3M} \hat{P}^T = \frac{1}{3} \left\{ |T_0\rangle \langle T_0| + |T_{+1}\rangle \langle T_{+1}| + |T_{-1}\rangle \langle T_{-1}| \right\} \otimes \frac{1}{M} \hat{I}_M, \quad (3)$$

291 where \hat{P}^T is the triplet projection operator, M is the total number of nuclear spin configurations,
292 $|T_0\rangle$ and $|T_{\pm 1}\rangle$ represent the triplet states of two electrons in RP with the spin magnetic quantum
293 number (m_S) equal to 0 and ± 1 respectively. \hat{I}_M represents the completely mixed initial state
294 of the nuclei.

295 The time dependence of the spin density operator is obtained using the Liouville Master
296 Equation [16, 40]:

$$\frac{d\rho(t)}{dt} = -\hat{L}[\rho(t)], \quad (4)$$

where Liouvillian superoperator $\hat{L} = \iota\hat{H} + \hat{K} + \hat{R}$. \hat{H} , \hat{K} , and \hat{R} are Hamiltonian superoperator, chemical reaction superoperator, and spin relaxation superoperator, respectively.

The most general spin Hamiltonian for RP will include Zeeman (\hat{H}_Z) and HF (\hat{H}_{HF}) interactions as well as the inter-radical interactions (\hat{H}_{IR}), which incorporate exchange and dipolar terms.

$$\hat{H} = \hat{H}_Z + \hat{H}_{HF} + \hat{H}_{IR}. \quad (5)$$

Due to the potential random orientation of the molecules in question, we only take into account the isotropic Fermi contact contributions in HF interactions. In this study we consider the following five isotropic HF couplings for FH[•]:

Nuclei	HFCC (μT)
H5	-802.9
N5	431.3
H8 (X3)	255.4

Table 1: Hyperfine interactions taken into account for FH[•] [30].

The unpaired electron on O₂^{•-} (containing two ¹⁶O nuclei) has no HF interactions. It should be noted that the fact that O₂^{•-} has no HFI helps in improving the magnetic sensitivity of RPs [41–44]. Furthermore, for simplicity, we do not consider any inter-radical interactions in our model. The form of the simplified spin Hamiltonian is given in Eq. 1

For spin-selective chemical reactions (reaction scheme of Fig. 1b), we use the Haberkorn superoperator [40], which is given by the following equation:

$$\hat{K} = \frac{1}{2}k_S(\hat{P}^S \otimes I_{4M} + I_{4M} \otimes \hat{P}^S) + \frac{1}{2}k_T(\hat{P}^T \otimes I_{4M} + I_{4M} \otimes \hat{P}^T), \quad (6)$$

where symbols have above stated meanings. Spin relaxation is modeled via random time-dependent local fields [45, 46], and the corresponding superoperator reads as follows:

$$\begin{aligned} \hat{R} = & r_A \left[\frac{3}{4}I_{4M} \otimes I_{4M} - \hat{S}_{Ax} \otimes (\hat{S}_{Ax})^T - \hat{S}_{Ay} \otimes (\hat{S}_{Ay})^T - \hat{S}_{Az} \otimes (\hat{S}_{Az})^T \right] \\ & + r_B \left[\frac{3}{4}I_{4M} \otimes I_{4M} - \hat{S}_{Bx} \otimes (\hat{S}_{Bx})^T - \hat{S}_{By} \otimes (\hat{S}_{By})^T - \hat{S}_{Bz} \otimes (\hat{S}_{Bz})^T \right], \end{aligned} \quad (7)$$

where the symbols have above stated meanings. The ultimate fractional O₂^{•-} yield for triplet-born RP ($\Phi_T^{(T)}$) for time periods much greater than the RP lifetime is given by:

$$\Phi_T^{(T)} = k_T \text{Tr} \left[\hat{P}^T \hat{L}^{-1} \left[\frac{1}{3M} \hat{P}^T \right] \right]. \quad (8)$$

The computational calculations and plotting were performed on Mathematica [47].

5.2 Animal care and amputations

An asexual clonal line of *Schmidtea mediterranea* (CIW4) was maintained in the dark at 18 °C. Planarians were kept in Ultrapure Type 1 water with Instant Ocean salts at 0.5 g/L (worm water). Animals were fed every third week with liver paste processed from a whole calf liver (antibiotic and hormone free) obtained from C. Roy & Sons Processing (Yale, MI). Liver paste was frozen and thawed only once. Worms 5-6 mm in length were used (which had been starved at least 2 weeks before use). Amputations were done with a scalpel over a custom made cooling peltier plate under a dissecting microscope. Fragments were produced via transverse amputation just anterior to the pharynx, with a single cut made at 90 degrees to the sagittal plane.

325 **5.3 Magnetic field exposure**

326 Experimentally-controlled static WMF exposures were generated with a custom-built MagShield
327 box (a pair of triaxial Helmholtz coils inside a partitioned mu-metal enclosure that blocks
328 external magnetic fields), as previously described [48]. Direct electric current to Helmholtz
329 coils was supplied by DC power sources (Mastech HY3005D-2-R) and was fed through both
330 x and y axis coils to produce a uniform magnetic field. The MagShield box was kept in a
331 temperature-controlled room (20 °C) and experiments were performed in the dark. Animals
332 were placed in 60 mm Petri dishes in worm water (or specific media as described), with a max
333 of $n = 10$ per replicate. For each replicate, 45 μT (Earth normal) controls were run in one
334 partition concurrently with experimental field strengths (as indicated) in the other partition.
335 Field strengths were confirmed using a milli/Gauss meter (AlphaLab models GM1-HS or MGM)
336 at the start and completion of each run. All planarians were exposed to WMFs within 5 min
337 of amputation and then continuously (except when dye solution was added) until they were
338 removed for imaging. Replicates (N) and total samples (n) per condition: 45 μT N = 15, n =
339 97; 0 μT N = 3, n = 26; 200 μT N = 6, n = 48; 500 μT N = 3, n = 29; 700 μT N = 2, n = 12;
340 900 μT N = 2, n = 20. Note: 0 μT = +/- 2 μT (tolerance of milligauss meter).

341 **5.4 Detection of superoxide and statistical analyses**

342 Superoxide levels were detected using a cell-permeant live fluorescent reporter dye as previously
343 described [12]. 2 μM orange 1 dye (Enzo Life Sciences ENZ-51012) in worm water used used,
344 made from 5 mM dimethylformamide stock; excitation, 550 nm; emission, 620 nm. Fragments
345 were exposed to WMFs from 5 min to 1 h post amputation. At 1 h, fragments were quickly
346 moved to new 35 mm Petri dishes in orange 1 solution and returned to the MagShield box for
347 an additional 1 h of WMF exposure. Thus fragments were exposed to WMFs for 2 h total,
348 including 1 h of dye loading, at which time regenerates were rinsed 3X in ice cold worm water
349 in the dark to preserve fluorescence and imaged. A Zeiss V20 fluorescence stereomicroscope with
350 an AxioCam MRm camera and ZEN (lite) software was used for image collection. Live images
351 were taken while fragments were extended to prevent signal intensity skewing due to scrunching.
352 Animals were imaged in 35 mm FluoroDishes (WPI FD35-100) with 25 mm round no. 1.5
353 coverslips (WPI 503508). All samples were imaged at the same magnification and exposure
354 levels to prevent confounding variables during comparisons (i.e., acquisition conditions were
355 kept constant across an experiment between control/treated). Photoshop (Adobe) was used
356 to orient and scale images. No data was added or subtracted. Original images available by
357 request. For quantification: the magnetic lasso tool in Photoshop was used to measure gray
358 mean values (signal intensity) of fluorescent dye at the anterior wound. To account for any
359 variation in dye loading, signal intensity was calculated as the difference between signal at the
360 anterior wound site versus signal from the middle of the regenerate (the pharyngeal region):
361 blastema – pharyngeal region. Significance: two-tailed Student's t-test with unequal variance
362 (Microsoft Excel) as compared to Earth normal controls.

Data availability

The original contributions presented in the study are included in the article/Supplementary Material, further inquiries can be directed to the corresponding author.

Code availability

The Mathematica notebooks used to generate theoretical plots are available from the corresponding author upon request.

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Author contributions

CS and WSB conceived the project; R performed the theoretical modelling and calculations with help from HZH and CS; JV performed planarian experiments; WSB and JV analyzed the planarian data; R and JV wrote the original draft with feedback from HZH, WSB and CS; R, JV, HZH, WSB and CS reviewed and edited the final version.

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Supporting Information

Multiple hyperfine interaction

We found that introducing a second HFI had significant effects, but adding additional HFIs beyond that had little impact.

Nuclei	HFCC (μT)
H5	-802.9
N5	431.3
H8 (X3)	255.4
N10	250.6
H β	190.8

Table 2: Hyperfine interactions for FH^* [30].

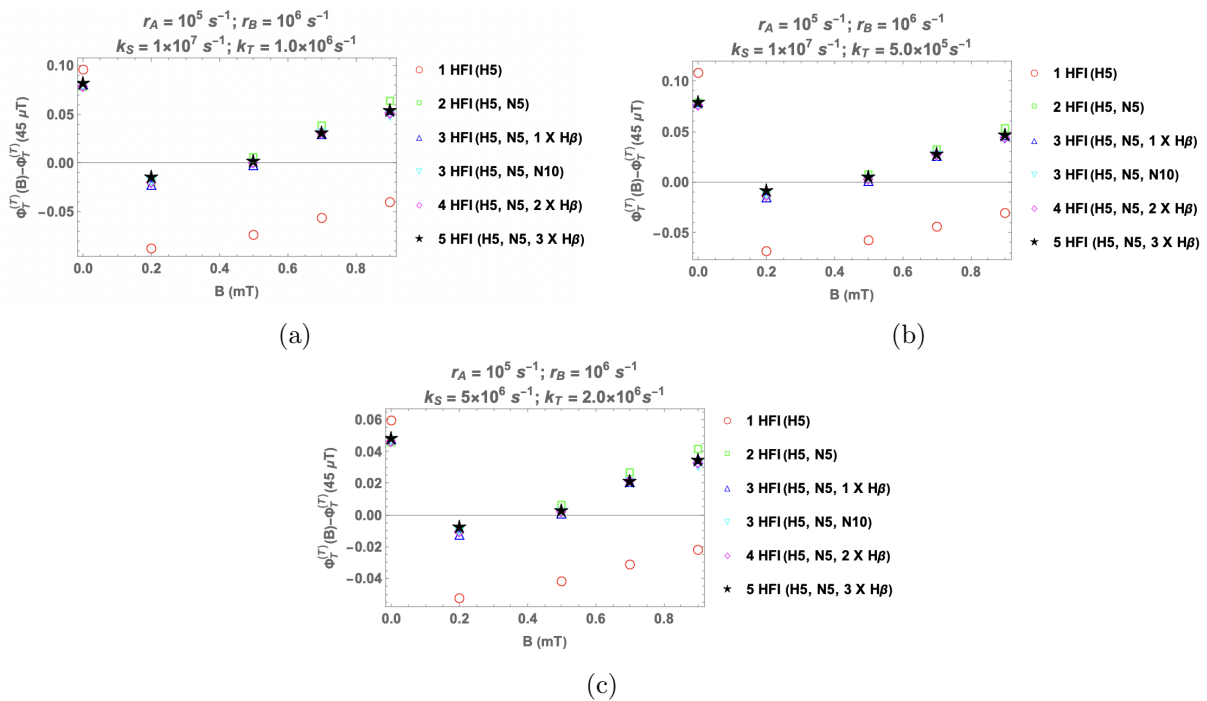


Figure 6: **Effects of having more than one HFIs:** Change in the fractional triplet yield for triplet-born RP with respect to the geomagnetic control ($45 \mu\text{T}$) as a function of the magnetic field. $r_A = 10^5 \text{ s}^{-1}$, $r_B = 10^6 \text{ s}^{-1}$. r_A and r_B are the spin relaxation rates of radicals A and B, respectively. k_S and k_T are singlet and triplet reaction rates, respectively. (a) $k_S = 10^7 \text{ s}^{-1}$ and $k_T = 10^6 \text{ s}^{-1}$, (b) $k_S = 10^7 \text{ s}^{-1}$ and $k_T = 5 \times 10^5 \text{ s}^{-1}$, (c) $k_S = 5 \times 10^6 \text{ s}^{-1}$ and $k_T = 2 \times 10^6 \text{ s}^{-1}$